

Discrete modeling of building structures geometric images

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Abstract

For discrete modeling of geometric images, it is possible to use the numerical method of finite differences, the static-geometric method, the mathematical apparatus of numerical sequences. Each of them has certain advantages and disadvantages, which depend on the solution of specific practical problems.

This article proposes to use the geometric apparatus of superpositions together with the above-mentioned methods. It allows significantly to improve the efficiency and expanding capacities of the process of geometric images discrete modeling. In particular, it makes it possible to investigate an opportunity of interpolating as parabolic functions as well as other elementary functional dependencies.

The purpose of this article is to expand capacities of the classical finite difference method and static-geometric method by using the geometric apparatus of superpositions. It allows using hyperbolic functions as interpolators for the geometric images discrete modeling. The result of this study is the obtained interpolating and extrapolating templates, which allow modeling geometric images of architectural and building constructions in a form of chain lines discrete frames.

Keywords: Discrete Modeling; Geometric Images; Finite Difference Method; Static-Geometric Method; Geometric Apparatus Of Superpositions.

1. Introduction

In the process of creating discrete modeling methods of architectural and building constructions geometric images of different problems must be solved. The most common problem is the problem of changing the discrete information about a geometric image into continuous and an inverse one. The first problem can be solved by interpolation methods. One of the most perspective directions of solving these problems is a wide usage of discrete geometric modeling methods [1, 2]. They allow significantly simplify algorithms and programs and to ensure the economy of computing resources.

It is proved that the theoretical axis of an arch corresponds as in the mirror to the shape of a thread, fixed in the bases of the arch [3].

This property allows using the shape of a sagging thread for building structures, which work both on compression and on stretching. Taking into consideration design static features give an opportunity to search for a form that corresponds to a minimum of unwanted stresses arising in it, and their concentrations. All this leads to the saving of building materials, which are used to provide additional rigidity and resistance to various loads.

A curve model is much easier to research than a surface model. It should be expected that a set of properties of a discrete line model can be transferred to a surface model, which is formed according to the same laws, if this line is considered as a component of the surface frame. Other properties of a discrete surface model can be obtained as a result of generalization of line model corresponding properties.

A sagging thread, evenly loaded in length, takes the form of a chain line. When an even load distributes along the horizontal axis, then

that thread takes the shape of a parabola. Changing a loading schedule of a thread, it becomes possible to manage its shape. This corresponds to one of the static-geometric method principles of constructing curve lines and contours [4]. Analytically, curve equations are obtained by double integration of a differential equation of the inextensible flexible thread equilibrium.

Another idealized interpretation of a thread as an absolutely extensible one allows to describe its shape in a discrete form analytically simply. The shape of a chain line resembles a parabola (Fig. 1, 2), but it is described by a hyperbolic cosine [5]:

$$y = a \cdot ch \frac{x}{a}. \quad (1)$$



Fig. 1. A chain that sags under its own weight

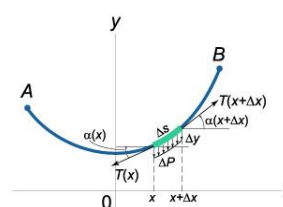


Fig. 2. A chain line with different parameter values

Its form is uniquely determined by parameter a , the dependence of which is shown in Figure 3. Chain lines are often found in nature and technology (Fig. 4). In architecture and construction, arches in the form of an inverted chain (Figs. 5, 6) have high stability due to the fact that internal compression forces are perfectly compensated and do not cause any deflection [6].

$$k_2 = \frac{(x_1 - x_3)(y_0 - y_3) - (x_0 - x_3)(y_1 - y_3)}{(x_1 - x_3)(y_2 - y_3) - (x_2 - x_3)(y_1 - y_3)}. \quad (5)$$

Table 1 shows a set of numerical sequence values (3) under condition $a=1$.

Table 1: The values of numerical sequence $y_i = ch i$

i	-7	-6	-5	-4	-3	-2	-1	0
y_i	548,31704	201,71564	74,20995	27,31823	10,06766	3,76220	1,54308	1
i	1	2	3	4	5	6	7	
y_i	1,54308	3,76220	10,06766	27,31823	74,20995	201,71564	548,31704	

By analogy with initial data for calculating right finite differences, we take the following coordinate of points:

1. $x_0 = 2; y_0 = 3,76220$; $x_1 = 3; y_1 = 10,06766$, $x_2 = 4; y_2 = 27,31823$; $x_3 = 5; y_3 = 74,20995$.

The values of superposition coefficients for calculating the ordinates of a desired point according to the ordinates of three adjacent points are determined by formulas (5):

1. $k_1 = 2,368667648918668$; $k_2 = -1,737335297837336$.
2. $x_0 = 3; y_0 = 10,06766$; $x_1 = 4; y_1 = 27,31823$, $x_2 = 5; y_2 = 74,20995$; $x_3 = 6; y_3 = 201,71564$.

The values of superposition coefficients are calculated by formulas (5):

1. $k_1 = 2,367986144430418$; $k_2 = -1,735972288860837$.
3. $x_0 = 4; y_0 = 27,31823$; $x_1 = 5; y_1 = 74,20995$; $x_2 = 6; y_2 = 201,71564$; $x_3 = 7; y_3 = 548,31704$;

the values of superposition coefficients are calculated by formulas (5):

1. $k_1 = 2,367893882454095$; $k_2 = -1,735787764908191$.
4. $x_0 = 5; y_0 = 74,20995$; $x_1 = 6; y_1 = 201,71564$, $x_2 = 7; y_2 = 548,31704$; $x_3 = 8; y_3 = 1490,47916$;

the values of superposition coefficients are calculated by formulas (5):

1. $k_1 = 2,367881395596904$; $k_2 = -1,735762791193807$.

As can be seen from the above four examples, the superposition coefficients of the three adjacent points will be the same up to the third decimal place. Therefore, as for polynomial curves, a computational template can be created for a discrete modeling of one-dimensional geometric images by interpolating the given nodal points by hyperbolic functions (similar to the templates of right finite differences). This template has a form:

$$\begin{aligned} 1 &= k_1 \oplus k_2 \oplus k_3; \\ 1 &= 2,368 \oplus -1,736 \oplus 0,368 \end{aligned} \quad (6)$$

By analogy with initial data for calculating central finite differences, we take the following coordinate of points:

1. $x_0 = 2; y_0 = 3,76220$; $x_1 = 1; y_1 = 1,54308$, $x_2 = 3; y_2 = 10,06766$; $x_3 = 4; y_3 = 27,31823$.

The values of superposition coefficients for calculating the ordinates of a desired point according to the ordinates of three adjacent points are determined from formulas (5):

1. $k_1 = 4,212848081925265 \cdot 10^{-1}$;
 $k_2 = 7,361455754224206 \cdot 10^{-1}$.
2. $x_0 = 3; y_0 = 10,06766$; $x_1 = 2; y_1 = 3,76220$, $x_2 = 4; y_2 = 27,31823$; $x_3 = 5; y_3 = 74,20995$;

the values of superposition coefficients are calculated by formulas (5):

1. $k_1 = 4,22178265683037 \cdot 10^{-1}$;
 $k_2 = 7,33465202950889 \cdot 10^{-1}$.
3. $x_0 = 4; y_0 = 27,31823$; $x_1 = 3; y_1 = 10,06766$, $x_2 = 5; y_2 = 74,20995$; $x_3 = 6; y_3 = 201,71564$;

the values of superposition coefficients are calculated by formulas (5):

1. $k_1 = 4,222997682448578 \cdot 10^{-1}$;
 $k_2 = 7,331006952654266 \cdot 10^{-1}$.
4. $x_0 = 5; y_0 = 74,20995$; $x_1 = 4; y_1 = 27,31823$, $x_2 = 6; y_2 = 201,71564$; $x_3 = 7; y_3 = 548,31704$;

the values of superposition coefficients are calculated by formulas (5):

$$\begin{aligned} k_1 &= 4,223162226187247 \cdot 10^{-1}; \\ k_2 &= 7,33051332143826 \cdot 10^{-1}. \end{aligned}$$

As can be seen from the above given examples, the superposition coefficients of the three adjacent points will be the same up to the third decimal place after the decimal point. Therefore, as for polynomial curves, a computational template can be created for discrete modeling of one-dimensional geometric images by interpolation of the given nodal points by hyperbolic functions (in analogy to the templates of central finite differences). This template has a form:

$$1 = 0,422 \oplus 0,733 \oplus -0,155. \quad (7)$$

The system of equations, which determinates the ordinates of sequence (3) nodal points by analogy with equations (4), has a form:

$$\begin{aligned} y_i - y_{i+2} &= k_1(y_{i-1} - y_{i+2}) + k_2(y_{i+1} - y_{i+2}) \\ y_{i+1} - y_{i+3} &= k_1(y_i - y_{i+3}) + k_2(y_{i+2} - y_{i+3}) \end{aligned} \quad (8)$$

From (8) expressions for calculating the values of superposition coefficients similar to formulas (5) are found:

$$\begin{aligned} k_1 &= \frac{(y_i - y_{i+2})(y_{i+2} - y_{i+3}) - (y_{i+1} - y_{i+2})(y_{i+1} - y_{i+3})}{(y_{i-1} - y_{i+2})(y_{i+2} - y_{i+3}) - (y_{i+1} - y_{i+2})(y_i - y_{i+3})}; \\ k_2 &= \frac{(y_{i-1} - y_{i+2})(y_{i+1} - y_{i+3}) - (y_i - y_{i+2})(y_i - y_{i+3})}{(y_{i-1} - y_{i+2})(y_{i+2} - y_{i+3}) - (y_{i+1} - y_{i+2})(y_i - y_{i+3})}. \end{aligned} \quad (9)$$

The values of superposition coefficients by formulas (9) were also calculated.

By analogy with initial data for calculating central finite differences, we take the following ordinates of points from Table 1:

1. $y_{i-1} = 3,762195691$, $y_i = 10,067662$, $y_{i+1} = 27,30823284$; $y_{i+2} = 74,20994852$.

1. $k_1 = 2,44728471054793 \cdot 10^{-1}$;
 $k_2 = 1,000000000000016$;

the values of superposition coefficients are calculated by formulas (9):

2. $y_{i-1} = 27,30823284$, $y_i = 74,20994852$, $y_{i+1} = 201,7156361$; $y_{i+2} = 548,3170352$,

the values of superposition coefficients are calculated by formulas (9):

1. $k_1 = 2,4472847105373753 \cdot 10^{-1}$;
 $k_2 = 1,000000000002819$.

As can be seen from the above examples, the superposition coefficients of the three adjacent points will be the same up to the twelfth decimal place (we can assume that they are equal). Therefore, as for polynomial curves, a computational template for a discrete modeling of one-dimensional geometric images can be created by interpolating given nodal points by hyperbolic functions. This template has a form:

$$1 = 0,244728471054 \oplus 1 \oplus -0,244728471054. \quad (10)$$

Or:

$$k_1 \oplus -1 \oplus k_2,$$

Or:

$$0,244728471054 \oplus -1 \oplus 1 \oplus -0,244728471054. \quad (11)$$

Example. We construct discrete models of curves with the following initial data:

1. $A(x_A=0, y_A=3)$; $B(x_B=3, y_B=1)$; $C(x_C=6, y_C=5)$;
2. $A(x_A=0, y_A=3)$; $B(x_B=3, y_B=0)$; $C(x_C=6, y_C=5)$;
3. $A(x_A=0, y_A=3)$; $B(x_B=3, y_B=-1)$; $C(x_C=6, y_C=5)$.

Taking into consideration a unit step along Ox axis, we compose the system of equations for all unknown nodes ($x_i = 1, 2, 4, 5$) of a numerical sequence model $y_i = ch i$:

$$\begin{cases} y_1 = 0,244728471054y_A + y_2 - 0,244728471054y_B \\ y_2 = 0,244728471054y_1 + y_B - 0,244728471054y_4 \\ y_B = 0,244728471054y_2 + y_4 - 0,244728471054y_5 \\ y_4 = 0,244728471054y_B + y_5 - 0,244728471054y_C \end{cases}$$

Substituting initial data 1, 2, 3 to that system, we have got the next results:

1. $y_1 = 1.551822587916218$; $y_2 = 1.062365645808218$; $y_4 = 1.296986501458353$;
 $y_5 = 2.275900385674355$;
2. $y_1 = 0.85644308351465$; $y_2 = 0.12225767035265$; $y_4 = 0.35687852600278$;
 $y_5 = 1.580520881272782$;
3. $y_1 = 0.16106357911308$; $y_2 = -0.81785030510292$; $y_4 = -0.58322944945279$; $y_5 = 0.88514137687121$.

The obtained discrete models of the curves according to the initial data are presented in Figure 6.

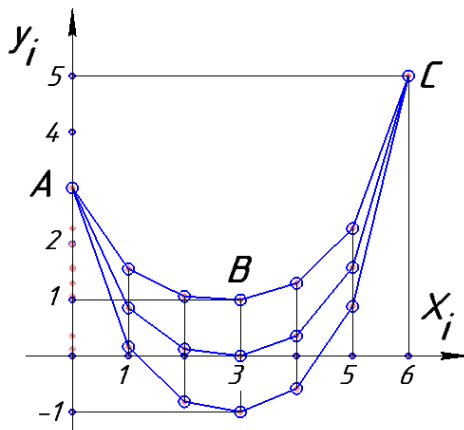


Fig. 9. Discrete models of the curves based on numerical sequence $y_i = \chi_i$.

Different problems of forecasting processes in various fields of science can be solved by extrapolation methods. For similar extrapolation problems it is better to use asymmetric computational templates. Templates (6), (7), (11) are asymmetric dependencies, which connect the ordinates of four adjacent nodes. The given node points are located on both sides from a desired point (on the right and on the left).

Let's input in formulae (9) the ordinates of four adjacent points, which are all located on one side from a desired point (for example, to the right from it):

$$\begin{aligned} k_1 &= \frac{(y_i - y_{i+3})(y_{i+3} - y_{i+4}) - (y_{i+2} - y_{i+3})(y_{i+1} - y_{i+4})}{(y_{i+1} - y_{i+3})(y_{i+3} - y_{i+4}) - (y_{i+2} - y_{i+3})(y_{i+1} - y_{i+4})} ; \\ k_2 &= \frac{(y_{i+1} - y_{i+3})(y_{i+1} - y_{i+4}) - (y_i - y_{i+3})(y_{i+2} - y_{i+4})}{(y_{i+1} - y_{i+3})(y_{i+3} - y_{i+4}) - (y_{i+2} - y_{i+3})(y_{i+1} - y_{i+4})} . \end{aligned} \quad (12)$$

The values of the adjacent points ordinates are taken from Table 1:

1. $y_i = 1,543080634815$; $y_{i+1} = 3,762195691084$;
 $y_{i+2} = 10,067661995778$;
 $y_{i+3} = 27,308232836016$; $y_{i+4} = 74,209948524788$.

The values of superposition coefficients for calculating the ordinates of a desired point according to the ordinates of three adjacent points will be determined by formulas (12):

1. $k_1 = 4,086161269652398$; $k_2 = -4,086161269660338$.
2. $y_i = 3,762195691084$; $y_{i+1} = 10,067661995778$;
 $y_{i+2} = 27,308232836016$;
 $y_{i+3} = 74,209948524788$; $y_{i+4} = 201,715636122456$.

The values of superposition coefficients are calculated by formulas (12):

1. $k_1 = 4,086161269312475$; $k_2 = -4,086161269195054$.
3. $y_i = 10,067661995778$; $y_{i+1} = 27,308232836016$;
 $y_{i+2} = 74,209948524788$;
 $y_{i+3} = 201,715636122456$; $y_{i+4} = 548,317035155212$.

The values of superposition coefficients are calculated by formulas (12):

$$k_1 = 4,08611270328305 ; k_2 = -4,086161270579006 .$$

As can be seen from the above given examples, the superposition coefficients of three adjacent points will be the same up to the eighth decimal place (they can be considered equal). Therefore a computational template for a discrete modeling of one-dimensional geometric images can be created by extrapolating the given nodal points to hyperbolic functions. This template has the form (13):

$$\begin{array}{c} (-1) \quad 4,08616127 \quad -4,08616127 \quad (1) \end{array} . \quad (13)$$

For interpolation problems it is better to have symmetric templates. The symmetric template can be formed in the next way.

The ordinates of five adjacent curve nodes will be connected by dependencies:

$$k_1 y_{i-2} - y_{i-1} + k_2 y_i + k_3 y_{i+1} = 0 \quad (14)$$

$$k_1 y_{i-1} - y_i + k_2 y_{i+1} + k_3 y_{i+2} = 0 \quad (15)$$

By analogy with the finite difference method, equations (14) and (15) can be reduced to one equation: $k_1 y_{i-2} - y_{i-1} - k_1 y_{i-1} + k_2 y_i + y_i + k_3 y_{i+1} - k_2 y_{i+1} - k_3 y_{i+2} = 0 \Rightarrow k_1 y_{i-2} - (1 + k_1) y_{i-1} + (1 + k_2) y_i + (k_3 - k_2) y_{i+1} - k_3 y_{i+2} = 0$

$$(16)$$

Considering that $-(1 + k_1) = (k_3 - k_2)$, $(1 + k_2) = 2$, equation (16) can be represented in the form of computational template (17):

$$\begin{array}{c} k_1 \quad k_3 - k_2 \quad 2 \quad k_3 - k_2 \quad k_1 \end{array} . \quad (17)$$

From (14) and (15) we have got the following:

$$0,244728471054 \cdot y_{i-2} - 1,244728471054 \cdot y_{i-1} + 2y_i - 1,244728471054 \cdot y_{i+1} + 0,244728471054 \cdot y_{i+2} = 0 . (18)$$

Or, in the form of computational template (19):

$$\begin{array}{c} 0,244728471054 \quad -1,244728471054 \quad 2 \quad -1,244728471054 \quad 0,244728471054 \end{array} . \quad (19)$$

Similarly, for example, equation (15), which connects the ordinates of four nodal points, can be formed from two equations (20) and (21), which link the ordinates of those points:

$$k_1 y_{i-1} - (k_2 + k_3) y_i + k_1 y_{i+1} = 0 , \quad (20)$$

$$k_1 y_i - (k_2 + k_3) y_{i+1} + k_1 y_{i+2} = 0 . \quad (21)$$

They can be represented in the form of symmetric computational template (22):

$$\begin{array}{c} k_1 \quad k_2 + k_3 \quad k_1 \end{array} . \quad (22)$$

Or (23):

$$\begin{array}{c} 0,244728471054 \quad -0,755271528946 \quad 0,244728471054 \end{array} . \quad (23)$$

Or, in the form of the recurrent formula:

$$0,244728471054 \cdot y_{i-1} - 0,755271528946 \cdot y_i + 0,244728471054 \cdot y_{i+1} = 0 . \quad (24)$$

Recurrent formula (24) allows discrete determination of the central nodal point ordinate (for two given adjacent points) of a modeling curve in the form of chain line sections. It also can interpolate by the function in form (3).

3. Conclusion

Based on the geometric apparatus of superpositions, computational templates for a discrete formation of geometric images by numerical sequences of hyperbolic functional dependences have been obtained. This extends capacities of discrete geometric modeling. Traditional methods of interpolation do not allow using transcendental functions as interpolants, because when substituting initial data we obtain the system of transcendental equations, which can not be solved in the general case.

The developed method allows conducting hyperbolic curves through the given points, which is impossible in most cases when using traditional interpolation methods.

The results of this work can be a base for further research on discrete formation of geometric images by one-dimensional numerical sequences of not only parabolic, hyperbolic, but also other elementary functional dependences. They also can be used for the formation of two-dimensional geometric images.

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